

MINISTRY OF EDUCATION AND SCIENCE OF UKRAINE

National aerospace university "Kharkiv Aviation Institute"

Department of aircraft strength

Course

Mechanics of materials and structures

HOME PROBLEM 12

Stress Analysis in Eccentric Tension – Compression

Name of student:

Group:

Advisor:

Data of submission:

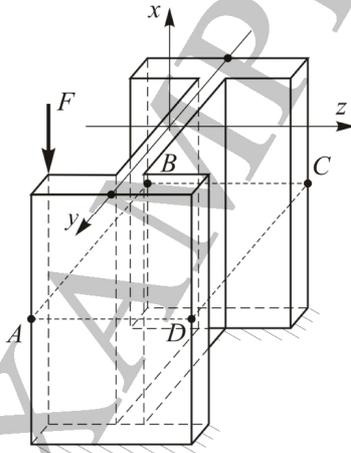
Mark:

**National aerospace university
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Subject: mechanics of materials
Document: home problem
Topic: stress analysis in eccentric tension – compression
Full name of the student, group

Variant: 11

Complexity: 1



Given: I-beam №(18), $F = 10 \text{ kN}$, $[\sigma] = 160 \text{ MPa}$.

Goal: 1) calculate stresses in an arbitrary cross – section $ABCD$ and check the strength; 2) Draw the graph of stress distribution in cross – section $ABCD$; 3) determine analytically position of neutral axis.

Full name of the lecturer

signature

Mark:

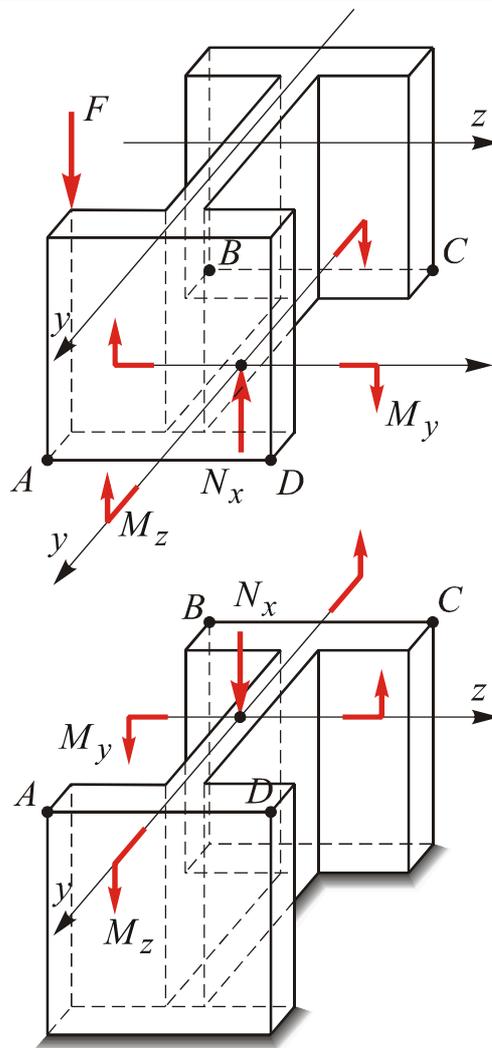


Fig. 2

Therefore,

$$\begin{aligned}\sigma_A &= -\sigma(N_x) - \sigma_{\max}(M_y) - \sigma_{\max}(M_z) = \\ &= -4.27 - 24.46 - 5.73 = -34.46 \text{ MPa},\end{aligned}$$

$$\sigma_B = -\sigma(N_x) - \sigma_{\max}(M_y) + \sigma_{\max}(M_z) = -4.27 - 24.46 + 5.73 = 23.00 \text{ MPa},$$

$$\sigma_C = -\sigma(N_x) + \sigma_{\max}(M_y) + \sigma_{\max}(M_z) = -4.27 + 24.46 + 5.73 = 25.92 \text{ MPa},$$

$$\sigma_D = -\sigma(N_x) + \sigma_{\max}(M_y) - \sigma_{\max}(M_z) = -4.27 + 24.46 - 5.73 = 14.46 \text{ MPa}.$$

3) Design the graph of stress distribution in $ABCD$ section in spatial cross section viewing with non-disturbed cross section for future geometrical analysis (see. Fig. 3).

4) Check the column strength:

(a) in tension, using the condition of strength

$$\sigma_{\max_t} \leq [\sigma]_t \rightarrow \sigma_{\max_t} = \sigma_C = 25.92 \text{ MPa} > 20 \text{ MPa}.$$

Conclusion: the column is non-strong in tension.

(b) in compression, using the condition of strength

$$|\sigma_{\max_c}| \leq [\sigma]_c \rightarrow |\sigma_{\max_c}| = |\sigma_A| = 34.46 \text{ MPa} < 80 \text{ MPa}.$$

Conclusion: the column is strong in compression.

General conclusion: the column is non-strong.

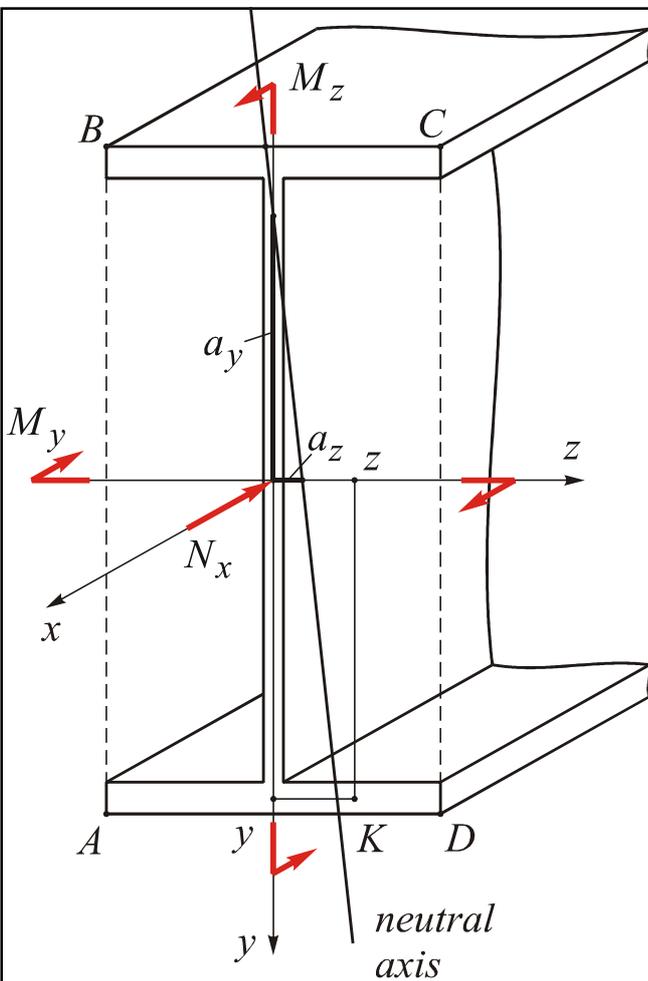


Fig. 4

$$\sigma_K = -\frac{N_x}{A} + \frac{M_y}{I_y} z - \frac{M_z}{I_z} y = 0$$

(this is equation of the plane in (σ, z, y) system of coordinates).

It may be rewritten as

$$Az + By + C = 0, \text{ where}$$

$$A = \frac{M_y}{I_y} = \frac{450}{82.6 \times 10^{-8}} = 5.45 \times 10^8,$$

$$B = -\frac{M_z}{I_z} = -\frac{819}{1290 \times 10^{-8}} = -0.63 \times 10^8,$$

$$C = -\frac{N_x}{A} = -\frac{10 \times 10^3}{23.4 \times 10^{-4}} = -0.43 \times 10^7.$$

Find the segments which the neutral axis cuts on the coordinate axes:

(a) in $z = 0$

$$y^* = a_y = -\frac{C}{B} = -\frac{-0.43 \times 10^7}{-0.63 \times 10^8} = -0.683 \times 10^{-1} \text{ m} = -68 \times 10^{-1} \text{ m} = -68 \text{ mm};$$

(b) in $y = 0$

$$z^* = a_z = -\frac{C}{A} = -\frac{-0.43 \times 10^7}{5.45 \times 10^8} = +0.079 \times 10^{-1} \text{ m} = +7.9 \times 10^{-3} \text{ m} = +7.9 \text{ mm}.$$

These segments are shown in scaled cross section sketch on Fig. 4. Finally, the neutral axis is drawn through the segments tips.

6) Check the solution accuracy, correlating the neutral axis positions on Figs. 3 and 4.